

TOTAL TIME FOR EXAMS IS ONE HOURS THIRTY MINUTES (1.30HR)

SECTION 1(VECTORS): 15 QUESTIONS ARE TO BE ANSWERED

^^ Determine the value of  $p$  so that the vectors  $2i + pj + k$  and  $4i - 2j - 2k$  perpendicular to each other.

@@ -3

@@ 3 ~

@@  $\frac{1}{3}$

@@  $-\frac{1}{3}$

@@None

^^If any two vectors  $\vec{a}$  and  $\vec{b}$  are parallel, then

@@  $\vec{a} \times \vec{b} = 0$

@@  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{a}$

@@  $\vec{a} \cdot \vec{b} = |\vec{a}||\vec{b}| \cos \theta$  ~

@@  $\vec{a} \times \vec{b} = -\vec{b} \times \vec{a}$

@@None

^^Which of the following is not a scalar quantity

@@ Mass

@@ Energy

@@ Density

@@ Pressure

@@ Weight ~

^^ The magnitude of a unit vector perpendicular to the plane of

$\vec{a} = 2\mathbf{i} - 6\mathbf{j} - 3\mathbf{k}$  and  $\vec{b} = 4\mathbf{i} + 3\mathbf{j} - \mathbf{k}$  is

@@ 2

@@ 0

@@ 1 ~

@@  $\sqrt{22}$

@@ None

^^ The unit vector parallel to the resultant of vectors  $\vec{a}_1 = 6\mathbf{i} - 3\mathbf{j} + 2\mathbf{k}$  and  $\vec{a}_2 = 3\mathbf{i} + \mathbf{j} - 2\mathbf{k}$  is

@@  $\frac{9\mathbf{i} + 2\mathbf{j}}{\sqrt{85}}$

@@  $\frac{9\mathbf{i} - 2\mathbf{j}}{\sqrt{85}}$  ~

@@  $\frac{-9\mathbf{i} + 2\mathbf{j}}{\sqrt{85}}$

@@  $\frac{-9\mathbf{i} - 2\mathbf{j}}{\sqrt{85}}$

@@ None

^^ For any unit vector  $\vec{q} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$ ,  $\vec{q} \cdot \vec{q}$  is

@@  $|\vec{q}|^2$

@@ 1 ~

@@  $q^2$

@@ 0

@@ None

^^ The projection of vector  $\vec{p}$  on another vector  $\vec{q}$  is

@@  $\frac{\vec{p} \times \vec{q}}{|\vec{p}|}$

@@  $\frac{\vec{p} \cdot \vec{q}}{|\vec{p}|}$

@@  $\frac{\vec{p} \cdot \vec{q}}{|\vec{q}|} \sim$

@@  $\frac{\vec{p} \times \vec{q}}{|\vec{p}| |\vec{q}|}$

@@ None

^^ The work done in moving an object along a vector  $3\vec{i} + \vec{j} - 5\vec{k}$  if the applied force is  $2\vec{i} - \vec{j} - \vec{k}$  is

@@ 5 units

@@ 33 units

@@ -5 units

@@ 10 units~

@@ None

^^ The cosine of the angle between  $\vec{a}_1 = \vec{i} + 2\vec{j} - \vec{k}$  and  $\vec{a}_2 = -4\vec{i} + \vec{j} - 2\vec{k}$  is

@@  $\pi$

$$@@ \frac{\pi}{3}$$

$$@@ \frac{\pi}{2} \sim$$

$$@@ \frac{\pi}{5}$$

$$@@ 2\pi$$

^^ The projection of a vector  $\vec{a}_1 = i - 2j + 3k$  on another vector  $\vec{a}_2 = i + 2j + 2k$  is

$$@@ \frac{1}{3}$$

$$@@ -\frac{1}{3}$$

$$@@ \frac{2}{3}$$

$$@@ 1 \sim$$

$$@@ 2i + 5k$$

^^ All of the following are properties of dot or scalar product except

@@ Commutativity

@@ Distribution of addition over multiplication

@@ Non-negative  $\sim$

@@ Associativity

@@ Bilinear

^^ If the dot product of two vectors  $\vec{a}_1$  and  $\vec{a}_2$  are non-zero, but  $\vec{a}_1 \cdot \vec{a}_2 = 0$ . Then the vectors are,

@@ Parallel to each other  $\sim$

@@ Perpendicular to each other

@@ Collinear

@@ Coplanar

@@ None

^^ For what value of  $m$  is the work-done by the force  $(1,1,1)$  on a particle which is displaced from  $(3,2,1)$  to  $(5,4,m)$  equals 20 units

@@ 10

@@ 15 ~

@@ 11

@@6

@@ None

^^ A particle moves along a curve whose parametric equations are  $x = e^{-t}$ ,  $y = 2t^2$ ,  $z = 2\cos t$  where  $t$  is time. The magnitude of velocity at  $t = 0$  is

@@ 0

@@ 1 ~

@@ -1

@@ 3

@@ None

^^ If  $\vec{a}_1 = 5it^2 + jt - t^3k$  and  $\vec{a}_2 = i\sin t - j\cos t$ . Then  $\left| \frac{d}{dt} (\vec{a}_1 \times \vec{a}_2) \right|_{t=0}$  is

@@ 0

@@ 1 ~

@@  $\sqrt{136}$

@@  $\sqrt{12}$

@@ None

^^ At what velocity should a body accelerating at  $2ti + 3t^2 + 2$  moves if the velocity is zero at  $t = 0$

@@  $t^2i + t^3j + 2tk \sim$

@@  $2t^2i + t^3j - 2tk$

@@  $2ti - t^2j + 3t^3k$

@@  $2t^2i + 3t^3j - 2tk$

@@ None

^^ The modulus of a vector  $\vec{p} = xi + yj + zk$  is given by

@@  $\vec{p} \cdot \vec{p}$

@@  $\sqrt{(x + y + z)^2}$

@@  $\sqrt{x^2 + y^2 + z^2} \sim$

@@  $|\vec{p}|$

@@ None

^^ The unit vector of the resultant of the vectors  $\vec{a}_1 = 3i + 2j - k$  and  $\vec{a}_2 = 2i - 2j - k$  is

@@  $\frac{5i - 2j}{\sqrt{25}}$

@@  $\frac{5i - 2k}{\sqrt{26}}$

@@  $\frac{5i - 2k}{\sqrt{29}} \sim$

@@  $\frac{5i + 2k}{\sqrt{29}}$

@@ None

^^ If the velocity of a particle moving along a curve is given by  $v = \cos at + j \sin bt + k 2t$ . What is the acceleration of the body at any time?

@@  $i \cos at + j \sin bt + 2k$

@@  $-i \cos at + j \sin bt - 2k$

@@  $i \sin at + j \cos bt - 2k$

@@  $-i \sin at + j \cos bt - 2k$  ~

@@ None

^^ Find the moment of the force represented by  $3i + k$  is acting through the point  $2i - j + 3k$  about the point  $i + 2j - k$ .

@@  $-3i + 11j - 9k$

@@  $-3i - j + 15k$

@@  $-3i + 11j + 9k$  ~

@@  $-3i + j + 15k$

@@ None

^^ All of the following are vectors except

@@ Acceleration

@@ Velocity

@@ Energy ~

@@ Momentum

@@ Friction.

^^ If  $\vec{a}$  is a non-zero vector, then the unit vector in its direction is expressed as

@@ 1

@@  $\frac{\vec{a}}{|\vec{a}|}$

@@  $\vec{a}$

@@  $\vec{a} \times 1$

$$\vec{a} \sim \frac{\vec{a}}{|\vec{a}|}$$

^^ If the three points with position vectors  $\vec{a}, \vec{b}, \vec{c}$  are collinear, and  $x\vec{a} + y\vec{b} + z\vec{c} = 0$ , then

@@  $x = y = z = 0$

@@  $x = y \neq z$

@@  $x = y + z$

@@  $x + y + z = 0 \sim$

@@ none

^^ If  $\vec{a}, \vec{b}, \vec{c}$  are non-coplanar, then  $x\vec{a} + y\vec{b} + z\vec{c} = 0$  implies

@@  $x = y = z = 0 \sim$

@@  $x = y \neq z$

@@  $x = y + z$

@@  $x + y + z = 0$

@@ none

^^ If the vector function  $\vec{u}(t)$  has a constant direction, then

@@  $\vec{u} \times \frac{d\vec{u}}{dt} = 0 \sim$

@@  $\vec{u} \cdot \frac{d\vec{u}}{dt} = 0$

@@  $\frac{d\vec{u}}{dt} = 0$

$$\frac{d\vec{u}}{dt} = \vec{u}$$

@@ none

^^ A particle moves along the curve  $x = a \cos(t)$ ,  $y = a \sin(t)$  and  $z = at \tan(y)$ . Find the magnitude of the acceleration at  $t = 0$

$$\text{@@ } a \cos t \mathbf{i} + a \sin t \mathbf{j} + at \tan y \mathbf{k}$$

$$\text{@@ } a \sec y$$

$$\text{@@ } a \sim$$

$$\text{@@ } 0$$

$$\text{@@ } a \csc y$$

^^ when using direction cosine method, which of the following is used in finding the angle between two vectors

$$\text{@@ } [l, m, n]$$

$$\text{@@ } \cos \theta$$

$$\text{@@ } l_1 l_2 + m_1 m_2 + n_1 n_2 \sim$$

$$\text{@@ } \cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{a}| |\vec{b}|}$$

@@ none

^^ If  $\vec{a} = 2\mathbf{i} + 4\mathbf{j} - 5\mathbf{k}$  and  $\vec{b} = \mathbf{i} + 2\mathbf{j} + 3\mathbf{k}$ , then the unit vector along  $\vec{a} + \vec{b}$  is

$$\text{@@ } \frac{3\mathbf{i} - 6\mathbf{j} - 2\mathbf{k}}{6}$$

$$@@ \frac{3\vec{i} + 6\vec{j} + 2\vec{k}}{7}$$

$$@@ \frac{4\vec{i} + 6\vec{j} + 2\vec{k}}{\sqrt{56}}$$

$$@@ \frac{\vec{i} + 2\vec{j} - 8\vec{k}}{\sqrt{69}}$$

$$@@ \frac{3\vec{i} + 6\vec{j} - 2\vec{k}}{7}$$

^^ If  $(\alpha - 5)\vec{a} + 3\alpha\vec{b}$  is parallel to  $4\vec{a} + 2\vec{b}$ , then  $\alpha$  is

@@ 1

@@ 2

@@ -1

@@ -2

@@ 3

^^ The direction cosines of the vector  $3\vec{i} - 4\vec{j} + 12\vec{k}$  are

$$@@ \frac{3}{13}, \frac{4}{13}, \frac{12}{13}$$

$$@@ \frac{3}{13}, \frac{-4}{13}, \frac{12}{13}$$

$$@@ \frac{3}{5}, \frac{4}{5}, \frac{12}{5}$$

$$@@ \frac{3}{5}, \frac{-4}{5}, \frac{12}{5}$$

@@  $\frac{3}{13}, \frac{-4}{13}, \frac{-12}{13}$

^^ If  $x\mathbf{i} - y\mathbf{j} + z\mathbf{k}$  is a unit vector then its direction cosines are

@@ l,m,n

@@ i,j,k

@@ 1,1,1

@@ x,y,z ~

@@ none

^^ The cosine of the angle between the vectors  $2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$  and  $6\mathbf{i} - 3\mathbf{j} + 2\mathbf{k}$  is

@@  $\frac{1}{3}$

@@  $\frac{1}{7}$

@@  $\frac{1}{21}$

@@  $\frac{4}{21}$  ~

@@  $\frac{20}{21}$

^^ If the vectors  $2\mathbf{i} + m\mathbf{j} + \mathbf{k}$  and  $6\mathbf{i} - 2\mathbf{j} - 2\mathbf{k}$  are perpendicular to each other, then m is

@@ 2

@@ 3

@@ 4

@@ 5 ~

@@ -3

^^ The projection of the vector  $2\mathbf{i} - 3\mathbf{j} - 6\mathbf{k}$  on the vector  $2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$  is

@@  $\frac{3}{4}$

@@  $\frac{4}{3}$  ~

@@ 4

@@ 3

@@ 12

^^ The vector projection of the vector  $2\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}$  on the vector  $\mathbf{i} + \mathbf{j} + \mathbf{k}$  is

@@  $3(2\mathbf{i} + 3\mathbf{j} + 4\mathbf{k})$

@@  $\frac{2\mathbf{i} + 3\mathbf{j} + 4\mathbf{k}}{\sqrt{3}}$

@@  $3(\mathbf{i} + \mathbf{j} + \mathbf{k})$  ~

@@  $\frac{\mathbf{i} + \mathbf{j} + \mathbf{k}}{\sqrt{3}}$

@@  $6\mathbf{i} + 9\mathbf{j} + 16\mathbf{k}$

^^ A man pushing a box exerts a force of 516.8N horizontally and 188.1N vertically downward. The box moves horizontally a distance of 20m. what is the work done on the box

@@ 516.8N

@@ 2556.2 units

@@  $-\frac{2556.2}{9}$  units

@@ 604.9 units

@@ 10336 units ~

^^ A unit vector perpendicular to the plane of  $2\vec{i} - 6\vec{j} - 3\vec{k}$  and

$4\vec{i} + 3\vec{j} - \vec{k}$  is

@@  $\frac{-3\vec{i} - 2\vec{j} + 6\vec{k}}{7}$

@@  $\frac{3\vec{i} - 2\vec{j} - 6\vec{k}}{7}$

@@  $\frac{1}{7}(3\vec{i} - 2\vec{j} + 6\vec{k}) \sim$

@@  $\frac{3\vec{i} + 2\vec{j} + 6\vec{k}}{7}$

@@  $-\frac{1}{7}(3\vec{i} + 2\vec{j} + 6\vec{k})$

^^ The area of a parallelogram with adjacent sides  $2\vec{i} + 4\vec{j} - 5\vec{k}$  and

$\vec{i} + 2\vec{j} + 3\vec{k}$  is (in square units)

@@  $11\sqrt{5}$

@@  $5\sqrt{11}$

@@  $\sqrt{55}$

@@  $12\sqrt{5}$

@@  $13\sqrt{5}$

^^ The vector moment about the point  $\vec{i} + 2\vec{j} + 3\vec{k}$  of a force  $\vec{i} + \vec{j} + \vec{k}$  acting at the point  $-2\vec{i} + 3\vec{j} + \vec{k}$  is

@@  $-3\vec{i} + \vec{j} - 4\vec{k}$

@@  $3\vec{i} - \vec{j} - 4\vec{k}$

@@  $3\vec{i} + \vec{j} - 4\vec{k} \sim$

@@  $3\vec{i} + \vec{j} + 4\vec{k}$

@@  $3\vec{i} - \vec{j} + 4\vec{k}$

^^ Find the linear velocity of a point P on the body with position vector relative to the point on the axis of rotation given by  $3\vec{i} + 2\vec{j} - \vec{k}$  if the angular velocity of the rotating body is  $5\vec{i} - 2\vec{j} + 3\vec{k}$ . is

@@  $\vec{i} + 3\vec{j} + 9\vec{k}$

@@ 10 units

@@  $8\vec{i} + 2\vec{k}$

@@  $\frac{4}{\sqrt{10}}(\vec{i} - 3\vec{j} - 9\vec{k})$

@@  $-4\vec{i} + 14\vec{j} + 16\vec{k} \sim$

^^  $|\vec{a} \times \vec{b}|^2 + (\vec{a} \cdot \vec{b})^2$  is

@@  $|\vec{a}|^2 + |\vec{b}|^2$

@@  $|\vec{a}|^2 - |\vec{b}|^2$

@@  $|\vec{a}|^2 + |\vec{b}|^2 \sim$

@@ None of these

^^ The area of a triangle whose vertices are, A(1,-1,2), B(2,1,-1) and C(3,-1,2) is

@@ 13

@@  $\sqrt{13} \sim$

@@ 6

@@  $\sqrt{6}$

@@ None

^^ If  $\vec{a}$  &  $\vec{b}$  are two non-zero vectors, then the component of  $\vec{b}$  along  $\vec{a}$  is

@@  $\frac{(\vec{a} \cdot \vec{b}) \vec{a}}{\vec{a} \cdot \vec{b}}$

@@  $\frac{(\vec{a} \cdot \vec{b}) \vec{b}}{\vec{a} \cdot \vec{a}}$

@@  $\frac{(\vec{a} \cdot \vec{b}) \vec{b}}{\vec{a} \cdot \vec{b}}$

@@  $\frac{(\vec{a} \cdot \vec{b}) \vec{a}}{\vec{a} \cdot \vec{a}} \sim$

@@ None

^^ If  $\vec{a} + \vec{b} + \vec{c} = 0$ , then the vectors  $\vec{a}$ ,  $\vec{b}$ ,  $\vec{c}$  satisfies one of the following relations

@@  $\vec{a} = \vec{b} = \vec{c} = 0$

@@  $\vec{a} \cdot \vec{b} = \vec{b} \cdot \vec{c} = \vec{c} \cdot \vec{a}$

@@  $\vec{a} \times \vec{b} = \vec{b} \times \vec{c} = \vec{c} \times \vec{a} \sim$

@@  $\vec{a} \times \vec{b} = -\vec{b} \times \vec{c} = \vec{c} \times \vec{a}$

@@ None

^^ A unit vector in the  $xy$ -plane which is perpendicular to  $4\vec{i} - 3\vec{j} + \vec{k}$  is

@@  $\frac{\vec{i} + \vec{j}}{\sqrt{2}}$

@@  $\frac{1}{5}(3\vec{i} + 4\vec{j}) \sim$

@@  $\frac{1}{5}(3\vec{i} - 4\vec{j})$

@@ None

^^ If the position vectors of the points A, B, C, D are

$2\vec{i} + 3\vec{j} + 5\vec{k}$ ,  $\vec{i} + 2\vec{j} + 3\vec{k}$ ,  $-5\vec{i} + 4\vec{j} - 2\vec{k}$ ,  $\vec{i} + 10\vec{j} + 10\vec{k}$  respectively, then:

@@  $\vec{AB} = \vec{CD}$

@@  $\vec{AB} \parallel \vec{CD} \sim$

@@  $\vec{AB} \perp \vec{CD}$

@@ None

^^ The points with the position vectors,  $60\mathbf{i} + 3\mathbf{j}$ ,  $40\mathbf{i} - 8\mathbf{j}$ ,  $a\mathbf{i} - 52\mathbf{j}$  are collinear if  $a$  is

@@  $-40$  ~

@@  $20$

@@  $-20$

@@  $10$

^^ The position vectors of a point  $C$  w.r.t  $B$  is  $\mathbf{i} + \mathbf{j}$  and that of  $B$  w.r.t  $A$  is  $\mathbf{i} - \mathbf{j}$ . Then the position vector of  $C$  w.r.t  $A$  is

@@  $2\mathbf{i}$  ~

@@  $2\mathbf{j}$

@@  $-2\mathbf{j}$

@@  $-2\mathbf{i}$

@@ None

^^ If the magnitude of  $\vec{a}$  and  $\vec{b}$  are equal and the angle between them is  $120^\circ$  and  $\vec{a} \cdot \vec{b} = -8$ , then  $|\vec{a}|$  is equal to

@@  $-5$

@@  $5$

@@  $4$  ~

@@  $2$

@@ None

^^ If  $3\mathbf{i} + 2\mathbf{j} + 5\mathbf{k}$  and  $2\mathbf{i} + \mathbf{j} - 3\mathbf{k}$  are the forces applied in displacing a particle from the point  $2\mathbf{i} - \mathbf{j} - 3\mathbf{k}$  to the point  $4\mathbf{i} - 3\mathbf{j} + 7\mathbf{k}$ . Then the work done by the force is

@@ 30 units

@@ 36 units

@@ 24 units ~

@@ 18 units

@@ None

^^ If  $(\vec{a} \times \vec{b})^2 + (\vec{a} \cdot \vec{b})^2 = 144$  and  $|\vec{a}| = 4$ , then  $|\vec{b}|$  is equal to

@@ 16

@@ 8

@@ 3 ~

@@ 12

@@ None

^^ If the sum of two unit vectors is a unit vector, then the magnitude of their difference is

@@  $\sqrt{1}$

@@  $\sqrt{2}$

@@  $\sqrt{3}$ ~

@@  $\sqrt{4}$

@@ None

^^ The rectangular unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  can have:

@@ a dot product equal to 1.

@@ a dot product equal to 0.~

@@ a dot product k.

@@ a negative dot product.

@@ None

^^ The rectangular unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  can have:

@@ a cross product with a magnitude equal to 1.

@@ a cross product equal to 0. ~

@@ a cross product  $-\mathbf{j}$ .

@@ a line in the same plane as their cross product

^^ If  $\mathbf{a}$  and  $\mathbf{b}$  are two non zero and non collinear vectors then  $\mathbf{a} + \mathbf{b}$  and  $\mathbf{a} - \mathbf{b}$  are:

@@ Linearly dependent vectors

@@ Coplanar vectors

@@ parallel vectors

@@ Linearly Independent vectors ~

@@ None

^^ Which one of the following represents a scalar quantity?

@@ The change in momentum of a rubber ball bouncing off the floor.

@@ The velocity of an airplane flying at 300 km/h on a bearing  $40^\circ$

@@ The speed of a car travelling at 100 km/h. ~

@@ The acceleration of an object thrown vertically upwards and which has reached the highest point of its motion.

@@ None

^^ The projection of the vector  $2\mathbf{i} - 3\mathbf{k}$  on the vector  $3\mathbf{i} + 4\mathbf{j}$  is

@@  $\frac{6}{5}$  ~

@@  $\frac{6}{3}$

@@ 9

@@ 16

@@  $\frac{5}{3}$

^^ If the vectors  $2\mathbf{i} - \mathbf{j} + \mathbf{k}$ ,  $\mathbf{i} + 2\mathbf{j} - 3\mathbf{k}$  and  $3\mathbf{i} + m\mathbf{j} + 5\mathbf{k}$  are

coplanar, the value of  $m$  is

@@ 4

@@ -4 ~

@@ 6

@@ -6

@@ 8

^^ A particle moves along the curve  $x = 5\cos t$ ,  $y = 5\sin t$ ,  $z = 5t^2$ , the magnitude of the acceleration at  $t = 0$  is

@@  $3\sqrt{5}$

@@  $4\sqrt{5}$

@@  $5\sqrt{5}$  ~

@@  $6\sqrt{5}$

@@  $7\sqrt{5}$

^^ The value of  $\vec{i} \cdot (\vec{j} \times \vec{k})$  is

@@  $\sqrt{3}$

@@ -k

@@ 3

@@ -1

@@ 1 ~

^^ The unit vector perpendicular to both  $\vec{a} = i + 2j - k$  and  $\vec{b} = 3i + 2j - k$  is

@@  $\frac{-(j+2k)}{\sqrt{5}}$  ~

@@  $\frac{-j+2k}{\sqrt{5}}$

@@  $\frac{(j-2k)}{\sqrt{5}}$

@@  $\frac{-(2j-4k)}{\sqrt{5}}$

@@ None

^^ For what value of  $m$  are the vectors  $2i+4j-k$  and  $mi+2j-2k$  perpendicular vectors

@@ 2

@@ 5

@@ 4

@@ -5 ~

@@ None

^^ A particle moves along the curve  $x=2t^2+1$ ,  $y=t^3$ ,  $z=t+4$ , what is its acceleration at time  $t=2$

@@  $4i+12j \sim$

@@  $6i-6j+k$

@@  $4i+12j+2k$

@@  $4i-2j$

@@ None

^^ A unit vector parallel to the resultant vector of vectors  $\vec{a}_1 = 6i - 3j + 2k$   
and  $\vec{a}_2 = 3i + j - 2k$

@@  $\frac{9i + 4j}{\sqrt{85}}$

@@  $\frac{9i - 4j}{\sqrt{85}}$

@@  $\frac{13i + 4j}{\sqrt{85}}$

@@  $\frac{9i - 2j}{\sqrt{85}} \sim$

@@ None

^^ Which of the following is a vector quantity

@@ momentum~

@@ energy

@@ power

@@ frequency

@@ None

^^ The points  $P(1, 2, 3)$ ,  $Q(-1, 2, -1)$  and  $R(1, -2, 3)$  are vertices of a triangle.

The area of the triangle is

@@  $2\sqrt{29} \sim$

@@  $3\sqrt{29}$

@@  $4\sqrt{29}$

@@  $5\sqrt{29}$

@@ None

^^ Let  $\vec{r} = 2i + j + 3k$  be a vector,  $|\vec{r} \times \vec{r}|$  is equal to

@@ 6

@@  $0 \sim$

@@ 4

@@ 5

@@ None

^^ Given that  $P(2,1,3)$ ,  $Q(1,4,5)$ ,  $R(2,5,3)$  and  $S(3,2,1)$  are the vertices of a parallelogram  $PQRS$ . The area of the parallelogram is

@@  $4\sqrt{2}$

@@  $4\sqrt{5} \sim$

@@  $5\sqrt{4}$

@@  $4\sqrt{3}$

@@ None

^^ The cosine of the angle between the vectors  $\vec{a}_1 = 5i + j - 2k$  and  $\vec{a}_2 = 4i - 4j + 3k$  is

@@  $0.2851 \sim$

@@ 0.8521

@@ 0.2158

@@ 0.5812

@@ None

^^ Let  $\vec{a}_1 = 5i + j - 2k$  be a vector with directional cosines  $\cos \alpha$ ,  $\cos \beta$  and  $\cos \gamma$  in the  $x, y, z$  directions respectively. Then  $\cos^2 \alpha + \cos^2 \beta =$

@@  $\frac{1}{5}$

@@  $\frac{11}{15}$

@@  $\frac{4}{5}$

@@  $\frac{13}{15}$  ~

@@ None

^^ For the unit vectors  $i, j, k$  in the directions of  $x, y, z$  respectively.  $i \times j \times k$  is equal to

@@ 1

@@ 3

@@ 0 ~

@@ -1

@@ None

^^ For the unit vectors  $i, j, k$  in the directions of  $x, y, z$  respectively.

$(i \times k) \times (k \times j)$  is equal to

@@ 1

@@ i

@@ k

@@  $-k$  ~

@@ None

^^ Let  $P$  and  $Q$  be two points with position vectors  $\vec{r}_1 = 6i - 3j + 2k$  and  $\vec{r}_2 = 3i + j - 2k$  respectively. The position vector of the point  $R$  which divides the line segment  $\overline{PQ}$  in the ratio  $2:3$  is

@@  $\vec{r} = \frac{9}{2}i - \frac{2}{3}j$

@@  $\vec{r} = \frac{9}{5}i - \frac{2}{5}j$

@@  $\vec{r} = \frac{24}{5}i - \frac{7}{5}j + \frac{2}{5}k$  ~

@@  $\vec{r} = \frac{21}{5}i - \frac{3}{5}j - \frac{2}{5}k$

@@ None

^^ The scalar projection of the vector  $\vec{a} = 3i - 2j + k$  on another vector  $\vec{b} = i + 2j - 3k$

@@  $\frac{2}{\sqrt{14}}$

@@  $\frac{-4}{\sqrt{14}}$  ~

@@  $\frac{3}{\sqrt{14}}$

@@  $\frac{4}{\sqrt{14}}$

@@ None

^^ If two forces  $F_1 = 3i + 5j + 6k$  and  $F_2 = 2i + 3j - 4k$  act on a body and displaced it by a distance  $d = 3i - 2j + 4k$ . The work done is equal to:

@@ 23

@@ -16

@@ 7 ~

@@ -7

@@ None

^^ If  $A$  and  $B$  have position vectors  $\vec{a} = 3i + 5j + 6k$  and  $\vec{b} = 2i + 3j - 4k$  then  $|2\vec{a} - 3\vec{b}|$

@@  $\sqrt{757}$

@@  $\sqrt{577}$  ~

@@  $\sqrt{230}$

@@  $\sqrt{332}$

@@ None

^^ If  $A$  and  $B$  have position vectors  $\vec{a} = 3i + 5j + 6k$  and  $\vec{b} = 2i + 3j - 4k$  then the vector  $\overrightarrow{BA}$  is

@@  $i + 2j + 10k$

@@  $-i - 2j - 10k \sim$

@@  $i + 2j + 3k$

@@  $-i - 2j + 10k$

@@ None

^^ The two vectors  $\vec{a} = 2i - 3j + k$  and  $\vec{b} = 4i + j - 5k$

@@ Parallel

@@ Perpendicular  $\sim$

@@ Linearly dependent

@@ Equal

@@ None

^^ A particle moves along a curve whose equation is  $x = 3t^3 + 2t$ ,  $y = t^3 - 2t$ ,  $z = t^2$ . Its acceleration at the instance of 2 seconds is

@@  $3i + 4j - 6k$

@@  $36i + 12j + 2k \sim$

@@  $2i + 36j + 12k$

@@  $3i - 36j + 2k$

@@ None

^^ A particle starts from rest with the velocity  $v = 3t^3 \underline{i} + 2t \underline{j} + t^2 \underline{k}$ . How far from the starting point is it at 2 seconds

@@  $3i + \frac{4}{3}j - 6k$

@@  $36i + 12j + 2k$

@@  $12i + 4j + \frac{8}{3}k \sim$

@@  $\frac{3}{8}i - 36j + 2k$

@@ None

^^ A particle moves along the curve with equation  $x = 2t^2 + 1$ ,  $y = t^2 + 2t$ ,  $z = t + 4$ . What is its acceleration at time  $t = 2$  seconds?

@@  $2i - 4j$

@@  $3i + 4j$

@@  $i + 2j$

@@  $4i - 2j \sim$

@@ None

^^ If the vector  $2i + 3j - 4k$  is perpendicular to  $4i + 8j + mk$ , the value of  $m$  is

@@  $8 \sim$

@@  $6$

@@  $9$

@@  $7$

@@ None

^^ A unit vector perpendicular to both  $\vec{a} = i + j$  and  $\vec{b} = j + k$  is

@@  $\frac{i - 2j - k}{\sqrt{2}}$

@@  $\frac{i - j + k}{\sqrt{3}} \sim$

@@  $\frac{i + j + k}{\sqrt{2}}$

@@  $\frac{i + 2j + k}{\sqrt{3}}$

@@ None

^^ The projection of  $\vec{p} = i + 2j - k$  and  $\vec{q} = 2i + 2j + k$  is

@@  $\frac{5}{\sqrt{2}}$

@@  $\frac{1}{\sqrt{5}}$

@@  $\sqrt{5} \sim$

@@  $\frac{2}{\sqrt{5}}$

@@ None

^^ If the vectors  $\vec{a} = 2i - 3j + k$  and  $\vec{b} = -2i - j + 2k$  are two sides of a triangle, the area of the triangle is

@@  $\frac{2\sqrt{5}}{5}$

@@  $\frac{5\sqrt{5}}{2} \sim$

@@  $\frac{3\sqrt{5}}{2}$

@@  $\frac{2\sqrt{5}}{3}$

@@ None

^^ If a force  $F = 2xz\mathbf{i} + xz\mathbf{j} - yx^2\mathbf{k}$  acted upon a particle and moves it from  $(0, 0, 0)$  to  $(1, 1, 1)$  along the curve  $x = t, y = t^2, z = t$ , the total work done by the force is

@@  $\frac{7}{10}$

@@  $\frac{8}{13}$

@@  $\frac{9}{11}$

@@  $\frac{13}{10} \sim$

@@ None

^^ Given that  $\vec{p} = e^t\mathbf{i} - 2\cos t\mathbf{j} + t^3\mathbf{k}$  and  $\vec{q} = 4t^2\mathbf{i} - 3e^t\mathbf{j} + \sin t\mathbf{k}$  find  $\left. \frac{d}{dt}(\vec{p} \cdot \vec{q}) \right|_{t=0}$

@@  $3 \sim$

@@  $e^t - 2\sin t$

@@  $e^t + \cos t$

@@ 5

@@ None

^^ The angle between the vectors  $\vec{a} = i + j + k$  and  $\vec{b} = 2i - 2j + 3k$  is

@@  $\frac{3}{\sqrt{17}}$

@@  $\frac{3}{\sqrt{51}} \sim$

@@  $\frac{3}{\sqrt{3}}$

@@  $\frac{3}{\sqrt{20}}$

@@ None

^^ The acceleration of a particle is given by  $\vec{a} = 4 \sin t i + 5 \cos 3t j - 7t^2 k$  Find its velocity at any time  $t$  if the velocity is zero at time  $t=0$

@@  $-4 \cos t i + \frac{5}{3} \sin 3t j - \frac{7}{3} t^3 k$

@@  $(2 - 4 \cos t) i + \frac{5}{3} \sin 3t j - \frac{7}{3} t^3 k$

@@  $(4 - 4 \cos t) i + \frac{5}{3} \sin 3t j - \frac{7}{3} t^3 k \sim$

@@  $-4 \cos t i + \left(3 + \frac{5}{3} \sin 3t\right) j - \frac{7}{3} t^3 k$

@@ None

^^ A parallelogram is formed with the vectors  $\vec{a} = -i - 3j + k$  and

$\vec{b} = 3i + 2j - 3k$ , the area of the parallelogram is

@@  $7\sqrt{2} \sim$

@@ 8

@@ 6

@@  $9\sqrt{3}$

@@ None

^^ The direction cosines of  $\vec{r} = i - 2j + 3k$  are

@@  $\frac{1}{\sqrt{6}}, \frac{-2}{\sqrt{6}}, \frac{3}{\sqrt{6}}$

@@  $\frac{1}{\sqrt{14}}, \frac{-2}{\sqrt{14}}, \frac{3}{\sqrt{14}} \sim$

@@  $\frac{1}{\sqrt{2}}, \frac{-2}{\sqrt{2}}, \frac{3}{\sqrt{2}}$

@@  $\frac{1}{\sqrt{11}}, \frac{-2}{\sqrt{11}}, \frac{3}{\sqrt{11}}$

@@ None

^^ What is the value of  $m$  if the vectors  $2i - 3j + mk$  and  $-i + \frac{3}{2}j + 9k$  are parallel to each other?

@@ 8

@@ 18

@@  $-18 \sim$

@@ -8

@@ None

^^ If  $A = (2, 3, 4)$  and  $B = (2, 2, 2)$  then  $\vec{BA} \cdot \vec{AB}$  equals to

@@ -5 ~

@@ 5

@@ 4

@@ 3

@@ None

^^ If  $A = (2, 3, 4)$  and  $B = (1, -2, 3)$  then  $\vec{AB} \times \vec{BA}$  equals to

@@ 1

@@  $i - 2j + 3k$

@@  $2i - 6j + 12k$

@@ 0 ~

@@ None

^^ If  $(i \times j) \cdot (j \times k) = P$  then  $2P$  equals to

@@ 0 ~

@@ 2

@@  $k \times i$

@@  $i \times k$

@@ None

^^ If the vectors  $ai + j$ ,  $j + k$  and  $i + k$  are linearly independent, the value of  $a$  equals to

@@ 1

@@ 2

@@ -1 ~

@@ -2

@@ None

^^ Let  $\vec{p} = i + j + k$  and  $\vec{q} = i + 2j - 3k$  be any two vectors. If the angle between  $\vec{p}$  and  $\vec{q}$  is  $\theta$  and the angle between  $\vec{p}$  and  $-\vec{q}$  is  $\alpha$ . Then,  $\theta + \alpha = ?$

@@  $\frac{\pi}{2}$

@@  $\pi$  ~

@@  $\frac{\pi}{4}$

@@  $2\pi$

@@ None

^^ If  $\vec{r} = \vec{p} \times \vec{q}$ , which of the following is true

I  $\vec{r} \cdot \vec{p} = \vec{r} \cdot \vec{q}$     II  $\vec{r} \cdot \vec{q} = 0$     III  $|\vec{r} \times \vec{p}| = |\vec{r}| |\vec{p}|$

@@ I only

@@ II and III only

@@ I and II only

@@ All of the above ~

@@ None

^^ The equation of the straight line which passes through the point  $P(1, 2, 3)$  and parallel to the vector  $\vec{v} = i + j - k$  is

@@  $i + j - k + \lambda(i + 2j + 3k)$

@@  $x + 1 = y + 2 = z - 3$

@@  $x - 1 = y - 2 = 3 - z \sim$

@@  $x - 2 = y - 3 = z - 2$

@@ None

^^ Given that  $\vec{p} = 2i + 2j + 2k$  and  $\vec{q} = 3i - 2j + k$ . The projection of  $\vec{p}$  on  $\vec{q}$  is

@@  $\frac{14}{\sqrt{14}} \sim$

@@  $\frac{14}{\sqrt{17}}$

@@  $\frac{17}{\sqrt{14}}$

@@  $\frac{17}{\sqrt{17}}$

@@ None

^^ A force  $F = 7i + 4j - 3k$  moves an object from  $(1, 2, 3)$  to  $(3, 2, 1)$ . The work done by the force is

@@ 14

@@ 22

@@ 20 ~

@@ 18

@@ None

^^ For any three vectors  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$ , if  $(\vec{p} \times \vec{q}) \cdot \vec{r} = 0$ . Which of the following is true?

I  $\vec{r}$  and  $\vec{p}$  are parallel

II  $\vec{r}$  and  $\vec{q}$  are perpendicular

III  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  are coplanar

IV  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  are collinear

@@ I and IV only

@@ II only

@@ III only ~

@@ II and III only

@@ None

^^ Let  $\vec{p}$  and  $\vec{q}$  be any two vectors, if  $|\vec{p} \times \vec{q}| = |\vec{p} \cdot \vec{q}|$  then the angle between  $\vec{p}$  and  $\vec{q}$  is

@@ 0

@@  $\frac{\pi}{4}$  ~

@@  $\pi$

@@  $\frac{\pi}{2}$

@@ None

^^ If  $\vec{p}$ ,  $\vec{q}$  and  $\vec{r}$  are coplanar,  $(\vec{p} \times \vec{q}) \times (\vec{p} \times \vec{r}) = ?$

@@  $\vec{p} \times (\vec{q} \times \vec{r})$

@@  $(\vec{p} \times \vec{p}) \times (\vec{q} \times \vec{r})$

@@  $0 \sim$

@@ 1

@@ None

^^ If  $\alpha$  is a scalar and  $\vec{p}$  and  $\vec{q}$  are vectors. Then,  $\alpha(\vec{p} \times \vec{q})$  is same as any one of the following.

I  $(\alpha\vec{p}) \times (\alpha\vec{q})$     II  $(\alpha\vec{p}) \times (\vec{q})$     III  $(\vec{p}) \times (\alpha\vec{q})$     IV  $\alpha(\vec{p} \cdot \vec{q})$

@@ II only

@@ I and III only

@@ II and IV only

@@ II and III only ~

@@ None

^^ Find the area of the triangle with vertices  $A(0,1,2)$ ,  $B(1,2,0)$  and

$C(2,0,1)$

@@  $\frac{2\sqrt{3}}{3}$

@@  $\frac{3\sqrt{2}}{2}$

@@  $\frac{3\sqrt{3}}{2} \sim$

@@  $\frac{2\sqrt{5}}{3}$

@@ None

^^ Given that the points  $P(1, 2, 3)$ ,  $Q(-2, -1, -3)$ ,  $R(2, 2, 2)$  and  $S(2, 1, 3)$  are points in space.  $P\vec{Q} + Q\vec{R} + R\vec{S} + S\vec{P} = ?$

@@  $0 \sim$

@@  $3i + 4j + 5k$

@@  $i + 2j + 3k$

@@  $i + j - k$

@@ None

^^ If the vectors  $\vec{a}$ ,  $\vec{b}$  and  $\vec{c}$  are sides of a triangle, which of the following is/are true

I  $\vec{a} + \vec{b} + \vec{c} = 0$     II  $|\vec{a} \times \vec{b}| = |\vec{c} \times \vec{a}|$     III  $|\vec{a} \times \vec{b}| = |\vec{b} \times \vec{c}|$

@@ I only

@@ I and III only

@@ I, II and III ~

@@ II and III only

@@ None

^^ Given that  $\vec{a} = 2i - 3j - k$  and  $\vec{b} = i + 4j - k$ . Evaluate  $(\vec{a} + \vec{b}) \times (\vec{a} - \vec{b})$

@@  $6i - 20j - 22k$

@@  $20i + 6j - 22k$

@@  $-20i - 6j - 22k$  ~

@@  $i + j - 3k$

@@ None

^^ A particle moves along a curve with parametric equation  $x = 8t^2 - 2t$ ,  $y = 2 \sin 2t$ ,  $z = 2 \cos t$ . The magnitude of its velocity at time  $t = 0$  is

@@  $5\sqrt{2}$

@@  $2\sqrt{5}$  ~

@@ 2

@@  $-2i + 4j$

@@ None

^^ A force  $\vec{F} = yz \underline{i} + xyz \underline{j} + x^2 y \underline{k}$  moves a particle along the curve,  $x = t$ ,  $y = 2t$  and  $z = t^2$  from  $(0, 0, 0)$  to  $(1, 2, 1)$ . The total work done by the force is

@@ 2.75

@@  $2\frac{1}{5}$

@@ 3.1

@@ 2.1 ~

@@ None

^^ Two vectors  $\vec{a}$  and  $\vec{b}$  of equal magnitude made angle  $60^\circ$  with each other. What is the magnitude of the vectors if  $\vec{a} \cdot \vec{b} = 8$

@@ 4 ~

@@ 2

@@ 6

@@ 3

@@ None

^^ The magnitude of two vectors  $\vec{a}$  and  $\vec{b}$  of equal magnitude is  $\sqrt{2}$ . What is the angle between them if  $\vec{a} \cdot \vec{b} = 1$

@@  $\frac{\pi}{2}$

@@  $\frac{\pi}{3}$  ~

@@  $\frac{\pi}{4}$

@@  $\frac{\pi}{6}$

@@ None

^^ If the points  $60\vec{i} + 3\vec{j}$ ,  $40\vec{i} + m\vec{j}$ ,  $-40\vec{i} - 52\vec{j}$  are collinear, the value of  $m$  is

@@  $-8$  ~

@@  $8$

@@  $4$

@@  $-4$

@@  $2$

^^ If the vectors  $2\vec{i} + 3\vec{j} - 4\vec{k}$ ,  $-\vec{i} + 2\vec{j} + \vec{k}$ ,  $\vec{i} + p\vec{j} - 7\vec{k}$  are coplanar, the value of  $p$  is

@@  $9$

@@  $19$  ~

@@  $6$

@@  $16$

@@  $18$

^^ If vectors  $x\vec{i} + 3\vec{j} + 2\vec{k}$ ,  $\vec{i} - 7\vec{j} - 8\vec{k}$ ,  $\vec{i} + \vec{j} - \vec{k}$  are linearly dependent, the value of  $x$  is

@@  $\frac{1}{9}$

@@  $\frac{1}{6}$

@@  $\frac{1}{3}$  ~

@@  $3$

@@  $6$

@@ The projection of the vectors  $2\vec{i} + 3\vec{j} + 4\vec{k}$  on the vector  $\vec{i} + \vec{j} + \vec{k}$  is

@@  $\sqrt{3}$

@@  $2\sqrt{3}$

@@  $3\sqrt{3} \sim$

@@  $4\sqrt{3}$

@@  $5\sqrt{3} \sim$

^^ If vectors  $2\vec{i} - \vec{j} + \vec{k}$  and  $\vec{i} + y\vec{j} - 5\vec{k}$  are perpendicular to another, the value of  $y$  is

@@ 1

@@ -1

@@ 2

@@ 3

@@ -3 ~

^^ A particle acted on by a constant force  $7\vec{i} + 2\vec{j} - 4\vec{k}$  is displaced from the point  $\vec{i} + 2\vec{j} + 3\vec{k}$  to the point  $5\vec{i} + 4\vec{j} + \vec{k}$ . The work done by the force is

@@ 40 units ~

@@ 30 units

@@ 25 units

@@ 20 units

@@ 10 units

^^ The moment about  $(1, -1, 1)$  of the force  $3\vec{i} + 4\vec{j} - 5\vec{k}$  acting at  $(1, 0, -2)$  is

@@  $7\vec{i} - 9\vec{j} - 3\vec{k} \sim$

@@  $7\vec{i} + 9\vec{j} - 3\vec{k}$

@@  $7\vec{i} - 9\vec{j} + 3\vec{k}$

@@  $7\vec{i} + 9\vec{j} + 3\vec{k}$

@@  $-7\vec{i} - 9\vec{j} - 3\vec{k}$

^^ A particle moves along the curve  $x = t^2, y = t^3 + 5, z = t + 1$ , where  $t$  is the time. The velocity of the particle at  $t = 1$  is

@@  $2\vec{i} - 3\vec{j} + 3\vec{k}$

@@  $2\vec{i} + 3\vec{j} + \vec{k} \sim$

@@  $3\vec{i} + 3\vec{j} + \vec{k}$

@@  $\vec{i} - 3\vec{j} + \vec{k}$

@@  $\vec{i} - 3\vec{j} - \vec{k}$

^^ If  $\vec{a} = t^4\vec{i} + t^3\vec{j} + t^2\vec{k}, \vec{b} = t^2\vec{i} + t^3\vec{j} + t^4\vec{k}$  when  $t = 1, \frac{d}{dt}(\vec{a} \cdot \vec{b})$  is

@@ 6

@@ 12

@@ 18 ~

@@ 24

@@ 30

^^  $\int_0^1 [3t^2\vec{i} + (4t^3 - 2t)\vec{j} + (5t^4 + t)\vec{k}] dt$  is

@@  $\vec{i} + \frac{3}{2}\vec{k} \sim$

@@  $\frac{3}{2}\vec{i} + \vec{k}$

@@  $\frac{3}{2}\vec{i} - \vec{k}$

@@  $\vec{i} - \frac{3}{2}\vec{k}$

@@  $-\vec{i} - \frac{3}{2}\vec{k}$

^^ The acceleration of a particle is given by  $12 \cos 2t\vec{i} - 8 \sin 2t\vec{j} + 16t\vec{k}$ . If its velocity is zero at  $t = 0$ , the velocity at anytime is

@@  $6 \sin 2t \vec{i} + 4(\cos 2t - 1) \vec{j} + 8t^2 \vec{k} \sim$

@@  $3 \sin 2t \vec{i} + 4(\cos 2t - 1) \vec{j} + 8t^2 \vec{k}$

@@  $6 \sin 2t \vec{i} + 3(\cos 2t - 1) \vec{j} + 8t^2 \vec{k}$

@@  $6 \sin 2t \vec{i} + 4(\cos 2t - 1) \vec{j} + 5t^2 \vec{k}$

@@  $6 \sin 2t \vec{i} + 4(\cos 2t + 1) \vec{j} + 8t^2 \vec{k}$

^^  $\vec{a} \times (\vec{b} + \vec{c}) + \vec{b} \times (\vec{c} + \vec{a}) + \vec{c} \times (\vec{a} + \vec{b})$  is equal to

@@  $\vec{a} + \vec{b} + \vec{c}$

@@  $\vec{a} - \vec{b} + \vec{c}$

@@  $\vec{a} + \vec{b} - \vec{c}$

@@  $\vec{0} \sim$

@@  $5 \vec{a}$

^^  $(\vec{a} - \vec{b})^2$  is equal to

@@  $\vec{a}^2 - \vec{b}^2$

@@  $\vec{a}^2 - 2\vec{a}\vec{b} + \vec{b}^2$

@@  $a^2 - 2\vec{a}\cdot\vec{b} + b^2 \sim$

@@  $\vec{a}^2 + 2\vec{a}\vec{b} + \vec{b}^2$

@@  $2(\vec{a} - \vec{b})$

^^ The vector perpendicular to both  $\vec{a}$  and  $\vec{b}$  is

@@  $\vec{a} - \vec{b}$

@@  $\vec{a} + \vec{b}$

@@  $\vec{a} \times \vec{b} \sim$

@@  $\frac{\vec{a}}{b}$

@@  $\vec{a}\vec{b}$

^^  $\vec{i} \cdot (\vec{j} \times \vec{k})$  is equal to

@@  $\vec{i}$

@@  $\vec{j}$

@@  $\vec{k}$

@@ 1 ~

@@ 0

^^ If  $x\vec{i} + 3\vec{j} - 5\vec{k}$  and  $2\vec{i} + 2\vec{j} + 2\vec{k}$  are mutually perpendicular, then  $x$  is

@@ 2 ~

@@ -2

@@ 4

@@ -4

@@ 3

^^ A unit vector perpendicular to each of the vectors  $\vec{i} + 2\vec{j} + 3\vec{k}$  and  $3\vec{i} + \vec{j} - \vec{k}$

@@  $\frac{1}{2}(\vec{j} + \vec{k})$

@@  $\frac{1}{\sqrt{2}}(\vec{j} + \vec{k})$  ~

@@  $\frac{1}{2}(\vec{j} - \vec{k})$

@@  $\frac{1}{\sqrt{2}}(\vec{j} - \vec{k})$

@@  $\vec{i} + \vec{j} + \vec{k}$

^^ The direction cosines of a vector  $\vec{i} - \vec{j} + \vec{k}$  are

@@  $\frac{1}{\sqrt{3}}, -\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} \sim$

@@  $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}$

@@  $\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, -\frac{1}{\sqrt{3}}$

@@  $-\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}$

@@  $\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}$

^^ The two vectors (-2,1) and (1,2) are

@@ linearly dependent of each other

@@ forming an orthonormal basis

@@ perpendicular to each other ~

@@ pointing in the opposite direction of each other e) none of the above.

^^ The scalar product (aka dot product) of two perpendicular vectors is A

@@ 0

@@ 1 ~

@@  $2\pi$

@@  $-2\pi$

@@ None

^^ If  $\lambda$  is a scalar value and  $\vec{v}$  and  $\vec{w}$  are two vectors in  $\mathbb{R}^3$ , then the result of

$\lambda (\vec{v} \times \vec{v}) \cdot (\vec{v} \times \vec{w})$  is

@@ a vector in  $\mathbb{R}^3$

@@ a scalar  $\sim$

@@ undefined

@@ a 3 by 3 matrix.

^^ If the angle between two vectors (both having a non-zero magnitude) is greater than  $90^\circ$  and smaller than  $270^\circ$ , then the scalar product (dot product) of these vectors is

@@ positive

@@ negative  $\sim$

@@ undefined

@@ positive when the angle is smaller than  $180^\circ$ , negative when the angle is greater than  $180^\circ$

^^ If the scalar product (dot product) of two unit vectors is zero, they are

@@ linearly dependent

@@ forming an orthonormal basis  $\sim$

@@ pointing in the same direction

@@ at an angle of  $180$  degrees to each other.

@@ None

^^ If ABCD is a parallelogram,  $\vec{AB} = 2\mathbf{i} + 4\mathbf{j} - 5\mathbf{k}$  and  $\vec{AD} = 2\mathbf{i} + 4\mathbf{j} - 5\mathbf{k}$ , then the unit vector in the direction of BD is

@@  $\frac{1}{\sqrt{69}}(\mathbf{i} + 2\mathbf{j} - 8\mathbf{k})$

@@  $\frac{1}{69}(\mathbf{i} + 2\mathbf{j} - 8\mathbf{k})$

@@  $\frac{1}{\sqrt{69}}(-i - 2j + 8k) \sim$

@@ None of these

^^ If C is the middle point of AB and P is any point outside AB, then

@@  $\vec{PA} + \vec{PB} = \vec{PC}$

@@  $\vec{PA} + \vec{PB} + \vec{PC} = 0$

@@  $\vec{PA} + \vec{PB} = 2\vec{PC} \sim$

@@  $\vec{PA} + \vec{PB} + 2\vec{PC} = 0$

^^ If the magnitude of  $\vec{a}$  and  $\vec{b}$  are equal and the angle between them is  $120^\circ$  and  $\vec{a} \cdot \vec{b} = -18$ , then  $|\vec{a}|$  is equal to

@@  $6 \sim$

@@  $4$

@@  $-6$

@@  $-4$

^^ If  $\theta$  is the angle between  $\vec{a}$  and  $\vec{b}$ , then  $\frac{(\vec{a} \cdot \vec{b})^2}{|\vec{a} \cdot \vec{b}|^2}$  is equal to

@@  $\tan^2\theta$

@@  $\cot^2\theta \sim$

@@  $1$

@@  $\sec^2\theta$

@@  $|\vec{a}|^2 |\vec{b}|^2$

**SECTION 2 (DYNAMICS) : ANSWER 15 QUESTIONS FROM THIS SECTION.**

^^ A particle is projected vertically upward from ground level with a velocity of  $50 \text{ m s}^{-1}$ . The maximum height attained by the particle is (take  $g = 10 \text{ m s}^{-2}$ )

@@ 50m

@@ 180m

@@ 100m

@@ 125m ~

@@ None

^^ A particle is projected vertically upward from ground level with a velocity of  $50\text{ m s}^{-1}$ . The time taken to attain a height of 100m when going up is (take  $g = 10\text{ m s}^{-2}$ )

@@  $5 + \sqrt{2}\text{ s}$

@@  $2 + \sqrt{2}\text{ s}$

@@  $5 - \sqrt{5}\text{ s} \sim$

@@ 3 s

@@ None

^^ A particle is projected vertically upward from ground level with a velocity of  $50\text{ m s}^{-1}$ . The total time taken for the particle to return to the ground is (take  $g = 10\text{ m s}^{-2}$ )

@@ 10 s ~

@@ 8 s

@@ 12 s

@@ 5 s

@@ None

^^ A particle is projected at an angle of  $60^\circ$  with the horizontal with an initial velocity of  $10\text{ m s}^{-1}$ . The greatest height attained by the particle is (take  $g = 10\text{ m s}^{-2}$ )

@@ 6 m

@@ 4.25 m

@@ 3.75 m ~

@@ 3.25 m

@@ None

^^ A particle is projected at an angle of  $60^\circ$  with the horizontal with an initial velocity of  $10 \text{ ms}^{-1}$ . The horizontal range of the projectile is (take  $g = 10 \text{ ms}^{-2}$ )

@@  $10\sqrt{3} \text{ m}$

@@  $10\sqrt{2} \text{ m}$

@@  $5\sqrt{2} \text{ m}$

@@  $5\sqrt{3} \text{ m} \sim$

@@ None

^^ A particle is projected at an angle of  $60^\circ$  with the horizontal with an initial velocity of  $10 \text{ ms}^{-1}$ . The total time of flight is (take  $g = 10 \text{ ms}^{-2}$ )

@@  $2\sqrt{3} \text{ s}$

@@  $\sqrt{3} \text{ s}$

@@  $3\sqrt{2} \text{ s}$

@@  $\sqrt{2} \text{ s}$

@@ None

^^ The resultant of two velocities  $u$  and  $v$  is  $\frac{v}{2}$  and perpendicular to  $u$ . The ratio of  $u$  and  $v$  is

@@  $\sqrt{3}:1$

@@  $\sqrt{2}:1$

@@  $\sqrt{3}:2 \sim$

@@  $\sqrt{3}:\sqrt{2}$

@@  $1:\sqrt{3}$

^^ The acceleration of a body moving with uniform velocity  $20 \text{ km/hr}$  after 2 hours will be (in  $\text{km/hr}^2$ )

@@ 40

@@ 20

@@ 10

@@ 5

@@ 0  $\sim$

^^ A bullet of mass  $0.006 \text{ kg}$  travelling at  $120 \text{ m/sec}$  penetrates  $x$  metre into a fixed target and is brought to rest in  $0.01 \text{ sec}$ , then  $x$  is (in cm).

@@ 3

@@ 6

@@ 9

@@ 30

@@ 60  $\sim$

^^ A particle is projected vertically upward with a velocity  $28 \text{ metre/sec}$ . Taking  $g=9.8 \text{ m/sec}^2$ , its Velocity after 2 seconds is (in metre/sec)

@@ 4.8

@@ 8.4  $\sim$

@@84

@@ 48

@@ 0.84

^^ A particle is projected vertically upward with a velocity 28 metre/sec. Taking  $g=9.8\text{m/sec}^2$ , its Position after 2 seconds is (in metre/sec)

@@ 3.64

@@ 34.6

@@36.4 ~

@@ 64.3

@@ 364

^^ A particle is projected vertically upward with a velocity 28 metre/sec. Taking  $g=9.8\text{m/sec}^2$ , its Maximum height attained is (in metre)

@@ 40 ~

@@ 50

@@60

@@ 70

@@ 80

^^ A particle is projected vertically upward with a velocity 28 metre/sec. Taking  $g=9.8\text{m/sec}^2$ , its Total time of flight is (in second)

@@  $\frac{10}{7}$

@@  $\frac{20}{7}$

@@  $\frac{30}{7}$

@@  $\frac{40}{7}$  ~

@@  $\frac{50}{7}$

^^ A particle is projected with a velocity of 49 meters/sec at an elevation of  $30^\circ$ . If  $g=9.8\text{m/sec}^2$ , then, the time of flight is

@@ 5 sec ~

@@ 10 sec

@@ 3 sec

@@ 6 sec

@@ 7 sec

^^ A particle is projected with a velocity of 49 meters/sec at an elevation of  $30^\circ$ . If  $g=9.8\text{m/sec}^2$ , then the horizontal range is

@@ 21.7m

@@ 212.17m ~

@@ 292m

@@ 29.2m

@@ 300m

^^ A particle is projected with a velocity of 49 meters/sec at an elevation of  $30^\circ$ . If  $g=9.8\text{m/sec}^2$ , the greatest height attained is

@@ 35.6m

@@ 38.6m

@@ 30.6m ~

@@ 25.6m

@@ 33.6m

^^ A particle is projected with a velocity of 49 meters/sec at an elevation of  $30^\circ$ . If  $g=9.8\text{m/sec}^2$ , if the greatest height attained by a projectile be equal to the horizontal range, then the angle of projection is

@@  $\tan^{-1} 2$

@@  $\tan^{-1} 3$

@@  $\tan^{-1} 4 \sim$

@@  $\tan^{-1} 5$

@@  $\tan^{-1} 6$

^^ A constant force acting in the direction of motion of a particle of mass 2 kg increases its speed from 4 m/sec to 20 m/sec in 4 seconds. Then the constant force is

@@ 4 N

@@ 2 N

@@ 40 N

@@ 8 N ~

@@ 16 N

^^ A string will break if the tension in it exceeds 10 N. If the maximum extension it can be given is  $\frac{1}{4}$  of its natural length, then its modulus of elasticity is

@@ 2.5 N

@@ 5 N

@@ 10 N

@@ 20 N

@@ 40 N ~

^^ The length of string of a seconds pendulum is

@@  $\frac{g}{\pi}$

@@  $\frac{g}{\pi^2} \sim$

@@  $\frac{\pi}{g}$

$$@@ \frac{\pi^2}{g}$$

$$@@ \frac{g}{2\pi^2}$$

^^ If the vector function  $\vec{a}(t)$  has constant direction, then

$$@@ \frac{d\vec{a}}{dt} = 0$$

$$@@ \vec{a} \cdot \frac{d\vec{a}}{dt} = 0$$

$$@@ \vec{a} \times \frac{d\vec{a}}{dt} = 0 \sim$$

$$@@ \frac{d\vec{a}}{dt} = 0$$

@@ none

^^ If the vector function  $\vec{a}(t)$  has constant magnitude, then

$$@@ \frac{d\vec{a}}{dt} = 0$$

$$@@ \vec{a} \cdot \frac{d\vec{a}}{dt} = 0 \sim$$

$$@@ \vec{a} \times \frac{d\vec{a}}{dt} = 0$$

$$@@ \frac{d\vec{a}}{dt} = 0$$

@@ none

^^ A particle moves along the curve  $x = a \cos t$ ,  $y = a \sin t$ ,  $z = at \tan \alpha$ , where  $a$  and  $\alpha$  are constant. The magnitude of its velocity at time  $t = 0$  is

@@  $a \cos \alpha$

@@  $a \sin \alpha$

@@  $a \sec \alpha$  ~

@@  $a \tan \alpha$

@@ zero

^^ Given that  $\vec{r}(t) = \begin{cases} 2\vec{i} - \vec{j} + 2\vec{k} & \text{when } t = 2 \\ 4\vec{i} - 2\vec{j} + 3\vec{k} & \text{when } t = 3 \end{cases}$  Then the value of

$\int_2^3 \vec{r} \cdot \frac{d\vec{r}}{dt} dt$  is

@@ 20

@@ 10 ~

@@ 5

@@ 25

@@ 30

^^ If  $\vec{F} = 3xy\vec{i} - y^2\vec{j}$  and  $C$  is the curve in the  $xy$ -plane  $y = 2x^2$  from  $(0, 0)$  to  $(1, 2)$ . Then the value of  $\int_C \vec{F} \cdot d\vec{r}$  is

@@  $\frac{7}{6}$

@@  $-\frac{7}{6}$  ~

@@  $\frac{6}{7}$

@@  $-\frac{6}{7}$

@@ 42

^^ Which of the following statements correctly describe the stretch of a spring?

@@ A greater stretching force produces a greater stretch

@@ A greater stretching force produces a greater force tending to return the spring to its original length

@@ If a stretch exceeds a spring's elastic limit, the spring will not return to its original length.

@@ all ~

^^ How are frequency and period related?

@@ frequency and period are equal

@@ frequency and period are reciprocals of each other ~

@@ frequency and period are unrelated

@@ additional information is needed

@@ None

^^ A new car bumper is designed to extend the time of impact by 3 times. This reduces the force of impact by

@@ about three times ~

@@ more than three times.

@@ about nine times.

@@ about 1.7 times.

@@ None

^^ A soldier fires a machine gun that shoots 10g bullets at a rate of 10 per second and a speed of 550 m/s. What is the average force of the gun on

the soldier?

@@ 0.3 N

@@ 12.6 N

@@ 110 N

@@ 55.0 N. ~

^^ If both the mass  $m$  of a simple pendulum and its length  $L$  are doubled, the period will

@@ increase by a factor of 1.4

@@ increase by a factor of 2.

@@ increase by a factor of 0.71.

@@ be unchanged. ~

@@ None

^^ Consider a mass hanging vertically from a spring and at equilibrium. If you pull it down by 2 cm and release it, it begins to oscillate at a frequency  $f_1$ . If you had pulled it down instead by 4 cm, what would its frequency of oscillation be ?

@@  $f_1/2$  ~

@@  $(\sqrt{2})f_1$

@@  $2f_1$ .

@@  $4f_1$ .

@@ None

^^ The horizontal and vertical components of the initial velocity of a football are 16 m/s and 20 m/s respectively. How long does it take for the football to rise to the highest point of its trajectory?

@@ 1.0 s

@@ 2.0 s ~

@@ 3.0 s

@@ 4.0 s

@@ None

^^ If two bodies are in direct elastic impact, then the coefficient of restitution  $e$  is

@@  $e = 1$

@@  $e > 1$

@@  $e < 1 \sim$

@@  $e = 0$

^^ A mass of 4kg is acted on by a force of 20N for 2sec. This force changes its velocity from  $u$  m/sec to 11m/sec, the value of  $u$  is

@@ 8

@@ 10  $\sim$

@@ 12

@@ 5

@@ 7

^^ If  $T$  be the time period of a simple pendulum of natural length  $L$ , then the frequency is

@@  $\frac{1}{2\pi} \sqrt{g/L} \sim$

@@  $2\pi \sqrt{L/g}$

@@  $\frac{1}{2\pi} \sqrt{g/L}$

@@  $2\pi \sqrt{L/g}$

^^ The path of a projectile in vacuum is a

@@ Straight line

@@ Circle

@@ Ellipse

@@ Parabola ~

@@ Hyperbola

^^ If string is stretched by two opposite forces of 10 N then tension in string is

@@ 5N

@@ 20 N

@@ 10 N

@@ Zero ~

@@ 1N

^^ To every action there is always an equal but opposite reaction, this statement is known as

@@ newton's 2nd law of motion

@@ newton's 1st law of motion

@@ newton's 3rd law of motion ~

@@ law of momentum

@@ law of action

^^ Push and pull that moves or tend to move, stops or tends to stop motion of a body is known as

@@ Force ~

@@ friction

@@ velocity

@@ momentum

@@ None

^^Acceleration that is produced by a 15N force in a mass of 8 kg will be equal to

@@  $1.5 \text{ ms}^{-2}$

@@  $1.87 \text{ ms}^{-2} \sim$

@@  $2.35 \text{ ms}^{-2}$

@@  $2 \text{ ms}^{-2}$

@@  $120 \text{ ms}^{-2}$

^^When a net force act on a body, it produces acceleration in body in direction of net force which is directly proportional to net force acting on body and inversely proportional to its mass. This statement is called

@@ newton's 2nd law of motion ~

@@ newton's 1st law of motion

@@ newton's 3rd law of motion

@@ law of momentum

^^ Quantity of motion that body possesses due to its mass and velocity is known as

@@ inertia

@@ momentum ~

@@ force

@@ friction

@@ weight

^^ A wire is stretched by 2 equal and opposite forces 15 N each. Tension in string will be

@@ 30 N ~

@@ 20 N

@@ 15 N

@@ 25 N

@@ None

^^ A force of 15 N moves a body with an acceleration of  $3 \text{ ms}^{-2}$ . Its mass is

@@ 10 kg

@@ 8 kg

@@ 12 kg

@@ 5 kg ~

@@ 45kg

^^ The moment taken about  $\vec{i} - \vec{j} + \vec{k}$  of a force  $2\vec{i} - \vec{j} + \vec{k}$  acting at  $\vec{i} + \vec{j} + \vec{k}$  is

@@  $2\vec{i} + 4\vec{k}$

@@  $2\vec{i} - 4\vec{k}$  ~

$$@@ \vec{2i} - 4\vec{j}$$

$$@@ \vec{2i} + 4\vec{j}$$

$$@@ \vec{2j} - 4\vec{k}$$

^^ A rigid body is spinning with angular velocity of 4 radians per second about an axis parallel to  $3\vec{j} - \vec{k}$  passing through the point  $\vec{i} + 3\vec{j} - \vec{k}$ . The linear velocity of the particle at the point  $4\vec{i} - 2\vec{j} + \vec{k}$  is

$$@@ \frac{4}{\sqrt{10}}(\vec{i} + 3\vec{j} + 9\vec{k})$$

$$@@ \frac{4}{\sqrt{10}}(\vec{i} + 3\vec{j} - 9\vec{k})$$

$$@@ \frac{4}{\sqrt{10}}(\vec{i} - 3\vec{j} + 9\vec{k})$$

$$@@ \frac{4}{\sqrt{10}}(\vec{i} - 3\vec{j} - 9\vec{k}) \sim$$

$$@@ \frac{\sqrt{10}}{4}(\vec{i} - 3\vec{j} - 9\vec{k})$$

^^ If string is stretched by two opposite forces of 10 N then tension in string is

$$@@ 5\text{N}$$

$$@@ 20\text{N}$$

$$@@ 10\text{N}$$

$$@@ \text{Zero} \sim$$

$$@@ 1\text{N}$$

^^ To every action there is always an equal but opposite reaction, this statement is known as

@@ newton's 2nd law of motion

@@ newton's 1st law of motion

@@ newton's 3rd law of motion ~

@@ law of momentum

@@ law of action

^^ Push and pull that moves or tend to move, stops or tends to stop motion of a body is known as

@@ Force ~

@@ friction

@@ velocity

@@ momentum

@@ None

^^ Acceleration that is produced by a 15N force in a mass of 8 kg will be equal to

@@  $1.5 \text{ ms}^{-2}$

@@  $1.87 \text{ ms}^{-2}$  ~

@@  $2.35 \text{ ms}^{-2}$

@@  $2 \text{ ms}^{-2}$

@@  $120 \text{ ms}^{-2}$

^^When a net force act on a body, it produces acceleration in body in direction of net force which is directly proportional to net force acting on body and inversely proportional to its mass. This statement is called

@@ newton's 2nd law of motion ~

@@ newton's 1st law of motion

@@ newton's 3rd law of motion

@@ law of momentum

^^ Quantity of motion that body possesses due to its mass and velocity is known as

@@ inertia

@@ momentum ~

@@ force

@@ friction

@@ weight

^^ A wire is stretched by 2 equal and opposite forces 15 N each. Tension in string will be

@@ 30 N ~

@@ 20 N

@@ 15 N

@@ 25 N

@@ None

^^A force of 15 N moves a body with an acceleration of  $3 \text{ ms}^{-2}$ . Its mass is

@@10 kg

@@8 kg

@@12 kg

@@5 kg ~

^^ Gravitational acceleration is acceleration of bodies

@@ on ground

@@ in air

@@ freely falling ~

@@ None

^^The time of ascent when measured from the point of projection of a body projected upwards , the

@@ Time of ascent > Time of descent

@@ Time of ascent < Time of descent

@@ Time of ascent=Time of descent. ~

@@ All of the above

@@ None

^^A ball tossed vertically upward rises, reaches its highest point, and then falls back to its starting point. During this time the acceleration of the ball is always

@@ in the direction of motion

- @@ opposite its velocity
- @@ directed downward ~
- @@ directed upward
- @@ None

^^If a particle is projected vertically upward with a velocity 28m/s. Taking  $g=9.8\text{m/s}^2$ , then its velocity after 2secs will be

- @@ 8.4m/s ~
- @@ 12m/s
- @@ 56m/s
- @@ 30m/s
- @@ 28m/s

^^If a particle is projected vertically upward with a velocity 28m/s. Taking  $g=9.8\text{m/s}^2$ , then its position after 2secs will be

- @@ 56.0m
- @@ 31.3m
- @@ 28m
- @@ 36.4m ~
- @@ 30m

^^If a particle is projected vertically upward with a velocity 28m/s. Taking  $g=9.8\text{m/s}^2$ , then its maximum height attained will be

- @@ 9.8m
- @@ 10m
- @@ 40m ~

@@ 56m

@@ None

^^If a particle is projected vertically upward with a velocity 28m/s. Taking  $g=9.8\text{m/s}^2$ , then its total time of flight will be

@@ 7.5secs

@@ 8.5secs

@@ 5.1secs

@@ 5.7secs ~

@@ 9.5secs

^^A change in momentum may result from

@@ an acceleration

@@ a force

@@ an impulse

@@ all of the above ~

@@ None